## STA130 Term Test - Section LEC0101

March 2, 2018

Last Name: $\qquad$ Last Name: $\qquad$

Student number: $\qquad$

Tutorial section or teaching assistant's name: $\qquad$

Instructions:

- Total marks: 45
- There are 11 pages including this page.
- Backs of pages will not be marked. Write your answers only in the space provided.
- The test is 90 minutes long.
- You are permitted a 1 -sided, handwritten, $8.5 \times 11$ inch aid sheet. You must hand in your aid sheet with your test.
- Calculators are not permitted.
- Questions begin on the next page.


## Question 1

[5 marks] Suppose you type commands into the R console as shown in the table below. For each of the $R$ commands, give the output that $R$ will produce, or an example of output that might be produced from the commands.

| R command | Output |
| :---: | :---: |
| 5+7 |  |
| $\begin{aligned} & \mathrm{vec}<-\mathrm{c}(2,6,7,11) \\ & \operatorname{vec}[2] \end{aligned}$ |  |
| $\begin{aligned} & \text { vec <- c(2, 6, 7, 11) } \\ & \text { quantile(vec, 0.5) } \end{aligned}$ |  |
| $\begin{aligned} & \mathrm{vec}<-\mathrm{c}(2,6,7,11) \\ & \text { sample(vec) } \end{aligned}$ |  |
| ```x <- rep(NA, 3) for (i in 1:3) { x[i] <- i } x``` |  |

## Data that will be used for the remainder of the questions

For the rest of this test, we will work with the ncbirths data set. This data set contains information on a random sample of 1000 births recorded in the state of North Carolina in 2004. The data set contains the following variables:

- fage: the age of the father in years at the time of the birth
- mage: the age of the mother in years at the time of the birth
- weeks: the length of the pregnancy in weeks
- premie: whether the birth was classified as premature (premie) or full term
- gained: weight gained by mother during the pregnancy in pounds
- weight: weight of the baby at birth in pounds
- gender: gender of the baby, female or male
- habit: status of the mother as a nonsmoker or a smoker

Here is a look at the data:

```
glimpse(ncbirths)
## Observations: 999
## Variables: 8
## $ fage <int> NA, NA, 19, 21, NA, NA, 18, 17, NA, 20, 30, NA, NA, NA,...
## $ mage <int> 13, 14, 15, 15, 15, 15, 15, 15, 16, 16, 16, 16, 16, 16,\ldots
## $ weeks <int> 39, 42, 37, 41, 39, 38, 37, 35, 38, 37, 45, 42, 40, 38,\ldots
## $ premie <fct> full term, full term, full term, full term, full term, ...
## $ gained <int> 38, 20, 38, 34, 27, 22, 76, 15, NA, 52, 28, 34, 12, 30,...
## $ weight <dbl> 7.63, 7.88, 6.63, 8.00, 6.38, 5.38, 8.44, 4.69, 8.81, 6...
## $ gender <fct> male, male, female, male, female, male, male, male, mal...
## $ habit <fct> nonsmoker, nonsmoker, nonsmoker, nonsmoker, nonsmoker, ...
table(ncbirths$premie)
##
## full term premie
## 846 152
table(ncbirths$gender)
##
## female male
## 502 497
table(ncbirths$habit)
##
## nonsmoker smoker
## 873 126
```

Questions about this data set begin on the next page.

## Question 2

[3 marks] For data wrangling, we have worked with the following functions:

- arrange()
- filter()
- group_by()
- mutate()
- select()
- summarise()

Name which of these functions is appropriate to use for each of the following tasks. You do not need to write the entire R command, just state which of the aobve functions you would use.
(a) Create the variable lowbirthweight with is "low" for babies whose birth weight (in the variable weight) is 5.5 pounds or less, and "not_low" for babies whose birth weight is greater than 5.5 pounds

Function to use: $\qquad$
(b) Remove the one observation that has a missing value of habit

Function to use: $\qquad$
(c) Create a dataset that includes only the variables that are measures on the mother and baby (and not the father)

Function to use: $\qquad$

## Question 3

(a) [2 marks] In ggplot we have used the following plotting geometries: geom_histogram(), geom_point(), geom_bar(), geom_boxplot()

Name which of these geometries would be appropriate to use to construct a plot that shows:
i. the distribution of gender

Geometry to use: $\qquad$
ii. the relationship between gained and weight

Geometry to use: $\qquad$
(b) [2 marks] One of the following histograms shows the distribution of weight and one shows the distribution of gained. One of the following boxplots shows the distribution of weight and one shows the distribution of gained.


## Boxplot 1



X

## Boxplot 2



Which histogram corresponds to which boxplot? Justify your answer.

## Question 4

In this question, we will investigate whether smoking during pregnancy has an effect on the gender of the baby. Specifically, we'll investigate whether the proportion of babies born who are girls is the same for smoking and non-smoking mothers. The table below summarizes the numbers of mothers who smoked or did not smoke while pregnant and the gender of their babies.

```
##
## female male
## nonsmoker 445 428
## smoker 57 69
```

(a) [2 marks] Why is this table of numbers not tidy data?
(b) [2 marks] We want to carry out an hypothesis test to investigate the question: Is the proportion of babies born who are girls the same for smoking and non-smoking mothers? State an appropriate null hypothesis. Define the parameter(s) you are testing.
(c) [2 marks] In order to carry out this hypothesis test, we will carry out a simulation. Indicate (by circling) whether each of the following statements about this simulation is TRUE or FALSE.
i. TRUE or FALSE: The distribution of the simulated values will be centred at $\frac{445}{445+428}-\frac{57}{57+69}$.
ii. TRUE or FALSE: For each simulated value, we first shuffle the values of habit in the original data.
(d) The simulation was run and the P -value for the test on the previous page is 0.27 .
i. [2 marks] Explain what is wrong with the following description of the P-value: "The probability that the null hypothesis is true is 0.27 ."
ii. [1 mark] Which one of the following statements is possibly true about this hypothesis test? Circle the statement.
A. We conclude that there is strong evidence that the proportion of babies who are females is different for smoking and non-smoking mothers. It is possible that the test resulted in a Type 1 error.
B. We conclude that there is no evidence that the proportion of babies who are females is different for smoking and non-smoking mothers. It is possible that the test resulted in a Type 1 error.
C. We conclude that there is strong evidence that the proportion of babies who are females is different for smoking and non-smoking mothers. It is possible that the test resulted in a Type 2 error.
D. We conclude that there is no evidence that the proportion of babies who are females is different for smoking and non-smoking mothers. It is possible that the test resulted in a Type $\mathbf{2}$ error.

## Question 5

Premature births occur in $12 \%$ of all births in the United States. In this question, we will conduct an hypothesis test to test whether we have evidence that the proportion of premature births in North Carolina is statistically different than the national proportion of $12 \%$. In our data, for the 998 observations for which we have a value of premie, 152 or $15.2 \%$ of babies are premature.

The R code for the simulation to carry out the hypothesis test is below. The values in simulated_stats are plotted below the code.

```
repetitions <- 100
simulated_stats <- rep(NA, repetitions)
for (i in 1:repetitions)
{
    new_sim <-
        sample(c("premie", "full_term"), size=n_observations,
                    prob=c(0.12, 0.88), replace=TRUE)
    sim_p <- sum(new_sim == "premie") / n_observations
    simulated_stats[i] <- sim_p
}
```

Plot of the values in simulated_stats


The questions regarding this output begin on the next page.
(a) i. [2 marks] If the null hypothesis changed, could you estimate the P -value for this test from this plot or would you need to run a new simulation? If yes, indicate how. If you need a new simulation, indicate which lines of code would need to change.
ii. [2 marks] If the test statistic changed, could you estimate the P-value for this test from this plot or would you need to run a new simulation? If yes, indicate how. If you need a new simulation, indicate which lines of code would need to change.
(b) [2 marks] Estimate the P-value as accurately as you can based on the plot.
(c) [8 marks] Summarize the results of the hypothesis test in a four to six sentence paragraph, using complete English sentences. The paragraph should address what is being tested, what was observed in the data, the P-value and what it means, and an appropriate conclusion. (If you don't know the P-value, pick a value to use to answer this question.)

## Question 6

In this question, we're interested in the mean weight of all baby boys in North Carolina.
(a) [1 mark] Which R code below creates a data frame that includes only boys and then creates a data frame that includes only the mean weight of the boys? Circle the correct code.
A.

```
boys <- ncbirths %>% select(gender == "male")
```

boys \% $>\%$ mutate (male_mean $=$ mean (weight))
B.

```
boys <- ncbirths %>% select(gender == "male")
```

boys \%>\% summarize(male_mean = mean(weight))
C.

```
boys <- ncbirths %>% filter(gender == "male")
```

boys \% \%\% summarize(male_mean = mean(weight))
D.
boys <- ncbirths \%>\% filter(gender == "male")
boys \%>\% mutate(male_mean $=$ mean(weight))
E.
boys <- ncbirths \%>\% group_by (gender)
boys \% \% \% summarize(male_mean = mean(weight))
F.

```
boys <- ncbirths %>% group_by(gender)
```

boys $\%>\%$ mutate (male_mean $=$ mean $($ weight $)$ )
(b) [2 marks] Is the mean produced by the correct code in part (a) a parameter or a statistic. Why?
(c) The data frame boys includes only the boys from the ncbirths data. The code below produces a bootstrap confidence interval for the mean weight of all baby boys in North Carolina (NC).

```
boot_means <- rep(NA, 5000)
sample_size <- as.numeric( boys %>% summarize( n() ) )
for (i in 1:5000)
{
    boot_samp <- ncbirths %>% sample_n(size = X1, replace=X2)
    boot_means[i] <- as.numeric( boot_samp %>% summarize(mean(weight)) )
}
quantile(boot_means, c(0.005, 0.995))
## 0.5% 99.5%
## 6.978888 7.222826
```

i. [2 marks] Two parts of the code have been replaced by X1 and X2. What should replace X1 and X 2 to correctly complete the code?

X1 should be $\qquad$ ; X2 should be $\qquad$
ii. [2 marks] Fill in the blanks based on the output of the code above (that is, the output that would be produced after X1 and X2 have been appropriately replaced):

A $\qquad$ \% confidence interval for the mean weight of all baby boys in NC is $\qquad$
(d) [2 marks] TRUE or FALSE. Circle the appropriate choice.
i. TRUE or FALSE: We would get a norrower confidence interval if there were more babies in the sample data.
ii. TRUE or FALSE: We would get a norrower confidence interval if we simulated more bootstrap samples.
(e) [1 mark] Suppose that a $95 \%$ confidence interval produced by the procedure in part (c) is (7.0, 7.2). A researcher interprets this confidence interval as follows: "With $95 \%$ confidence, we can infer that a randomly chosen North Carolina baby will weigh between 7.0 and 7.2 pounds." Why is the researcher's interpretation of the confidence interval incorrect? Circle the best answer.
A. Because the babies in the sample could be many possible weights, including values less than 7.0 pounds and greater than 7.2 pounds.
B. Because the confidence interval estimates weight for the sample and not for the population.
C. Because the confidence interval estimates the mean weight in the population and not the weight of an individual baby.
D. Because $95 \%$ of babies born in North Carolina will weigh between 6.98 and 7.22 pounds.

