## STA130H1S - Week #10

Another variable can affect the nature of a relationship

Prof. A. Gibbs March 19, 2018

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### **Today**

#### Big idea:

Examining the affect of another variable on a relationship

#### Important concepts:

- 1. Inference for regression parameters
- 2. Regression when the independent variable is a categorical variable
- 3. Is the regression line the same for two groups?
- 4. An example of a variable affecting a relationship in a non-regression setting
- 5. Confounding

#### Recommended reading:

Section 7.6 of *Modern Data Science with R*Section 1.4.1 of *Introductory Statistics with Randomization and Simulation* from OpenIntro



#### What affects course evaluations?

... other than the quality of the course ...

- Data from course evaluations for a random sample of courses at the University of Texas at Austin.
- Each observation corresponds to a course.
- score is the average student evaluation for the course.
- bty\_avg is the average beauty rating of the professor, based on ratings of physical appear from 6 students in the course.

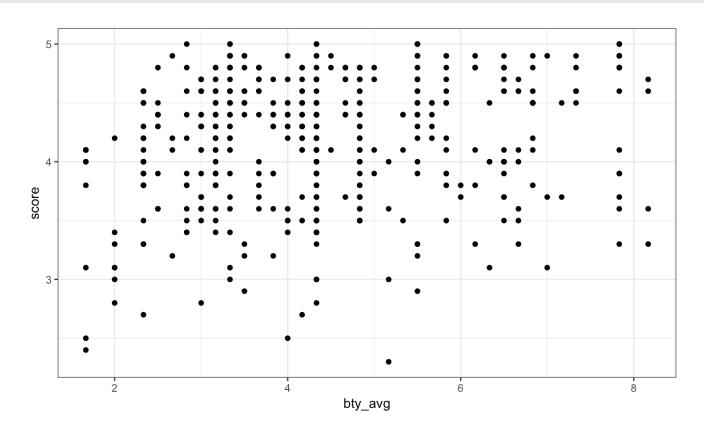
```
download.file("http://www.openintro.org/stat/data/evals.RData", destfile = "evals.RData")
load("evals.RData")
```

#### glimpse(evals)

```
## Observations: 463
## Variables: 21
## $ score
                   <dbl> 4.7, 4.1, 3.9, 4.8, 4.6, 4.3, 2.8, 4.1, 3.4, 4.5...
## $ rank
                   <fctr> tenure track, tenure track, tenure track, tenur...
## $ ethnicity
                   <fctr> minority, minority, minority, minority, not min...
## $ gender
                   <fctr> female, female, female, male, male, male, male...
## $ language
                   <fctr> english, english, english, english, english, en...
## $ age
                   <int> 36, 36, 36, 36, 59, 59, 59, 51, 51, 40, 40, 40, ...
## $ cls perc eval <dbl> 55.81395, 68.80000, 60.80000, 62.60163, 85.00000...
## $ cls did eval
                   <int> 24, 86, 76, 77, 17, 35, 39, 55, 111, 40, 24, 24,...
## $ cls students
                   <int> 43, 125, 125, 123, 20, 40, 44, 55, 195, 46, 27, ...
## $ cls level
                   <fctr> upper, upper, upper, upper, upper, upper, upper...
## $ cls profs
                   <fctr> single, single, single, multiple, multi...
## $ cls credits
                   <fctr> multi credit, multi credit, multi credit, multi...
## $ bty fllower
                   <int> 5, 5, 5, 5, 4, 4, 4, 5, 5, 2, 2, 2, 2, 2, 2, 2, ...
## $ bty flupper
                   <int> 7, 7, 7, 7, 4, 4, 4, 2, 2, 5, 5, 5, 5, 5, 5, 5, ...
                   <int> 6, 6, 6, 6, 2, 2, 2, 5, 5, 4, 4, 4, 4, 4, 4, 4, ...
## $ bty f2upper
## $ bty m1lower
                   <int> 2, 2, 2, 2, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 3, ...
                   <int> 4, 4, 4, 4, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, 3, ...
## $ bty mlupper
## $ bty m2upper
                   <int> 6, 6, 6, 6, 3, 3, 3, 3, 2, 2, 2, 2, 2, 2, 2, ...
## $ bty avg
                   <dbl> 5.000, 5.000, 5.000, 5.000, 3.000, 3.000, 3.000,...
## $ pic outfit
                   <fctr> not formal, not formal, not formal, not formal,...
```

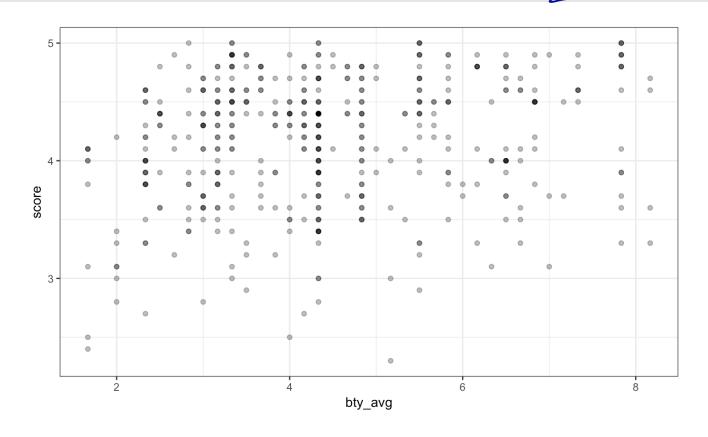
## Relationship between score and bty\_avg?

ggplot(evals, aes(x=bty\_avg, y=score)) + geom\_point() + theme\_bw()



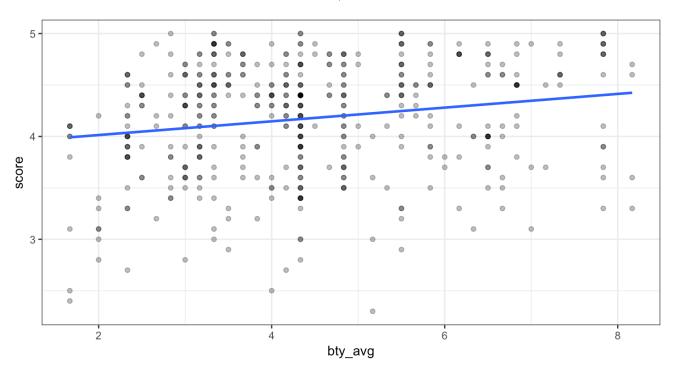
Use some transparency so we can see where there are overlapping points

```
ggplot(evals, aes(x=bty_avg, y=score)) + geom_point(alpha=0.3) + theme_bw()
```

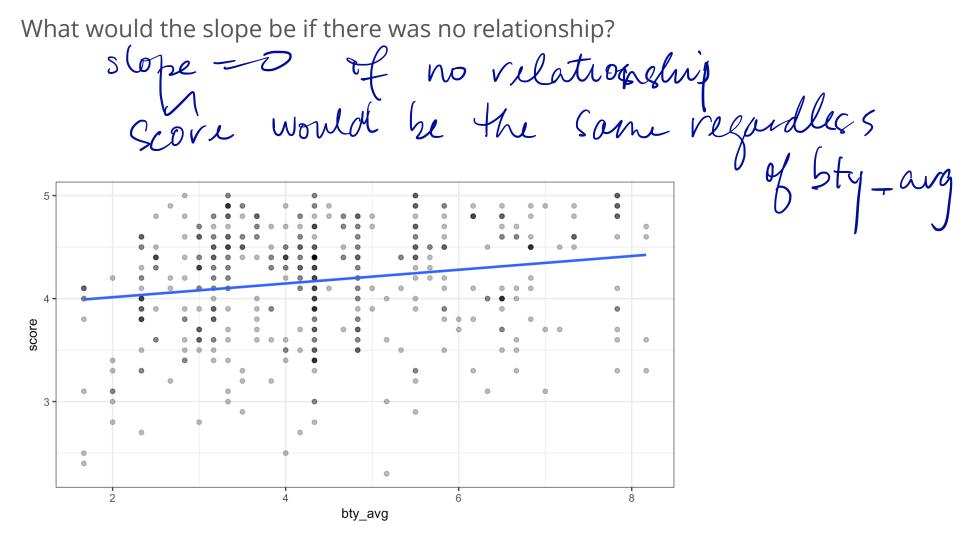


#### Is there a relationship between score and bty\_avg?

```
ggplot(evals, aes(x=bty_avg, y=score)) + geom_point(alpha=0.3) + theme_bw() +
geom_smooth(method = "lm", fill=NA)
```

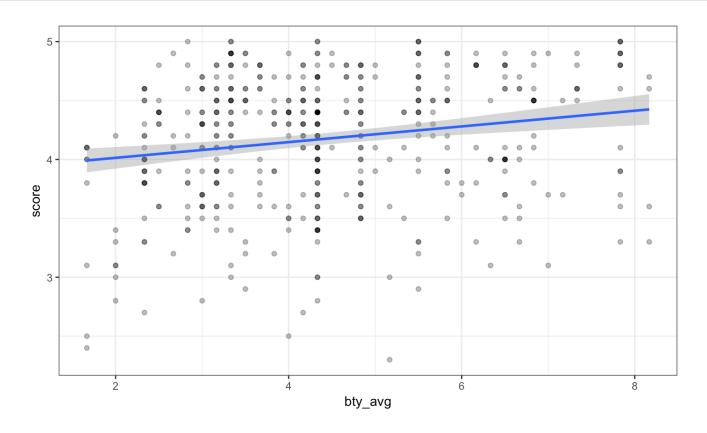


What would the slope be if there was no relationship?



By default, geom\_smooth gives a confidence interval for the fitted line (or curve)

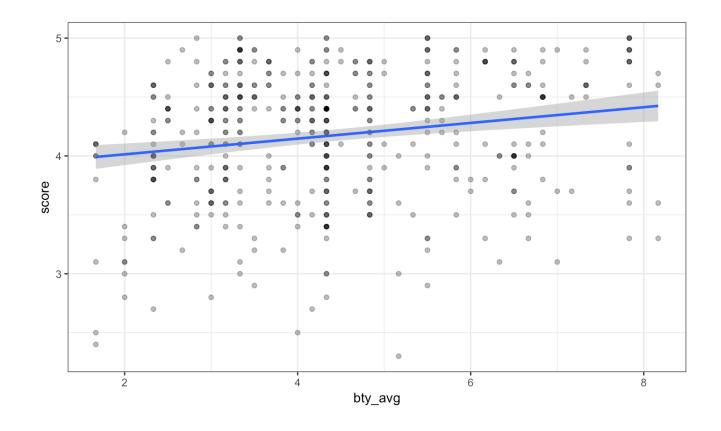
```
ggplot(evals, aes(x=bty_avg, y=score)) + geom_point(alpha=0.3) + theme_bw() +
geom_smooth(method = "lm")
```



## Inference for regression part 1: Confidence interval for the slope

The grey shaded area around the fitted regression line is a 95% confidence interval for the slope. Why

- The width of the confidence interval varies with the independent variable bty\_avg.
- The confidence interval is wider at the extremes; the regression is estimated most precisely near the mean of the independent variable.
- The confidence interval for the slope shown is calculated based on a probability model that assumes all observations are independent and that the error terms have a symmetric, bell-shaped distribution.
- · Confidence intervals for the slope can also be calculated using the bootstrap.



Does the confidence interval indicate that 0 is a possible value for  $\beta_1$  (the parameter for the slope)?

No hovizontal line doesn't fit in the grey bands

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# Inference for regression part 2: Hypothesis test for the slope

Output from the summary command for the estimated regression coefficients:

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 3.88033795 0.07614297 50.961212 1.561043e-191
## bty_avg 0.06663704 0.01629115 4.090382 5.082731e-05
```

- The estimate of the slope is 0.06664.
- When using the 1m function, by default the P-value is calculated based on a probability model that assumes all observations are independent and that the error terms have a symmetric, bell-shaped distribution.
- The P-value is  $5.08 \times 10^{-5} = 0.0000508$

Does the hypothesis test for the slope indicate that the slope is different from 0?

We have strong widence that the slope is not D, so there is a relationship between sove set and bety-aug

## What other factors might affect course evaluations?



Topics **✓** 

**Current edition** 

More ~

Academic sexism

## Research suggests students are biased against female lecturers

How long does that prejudice last?

Print edition | Science and technology >
Sep 21st 2017







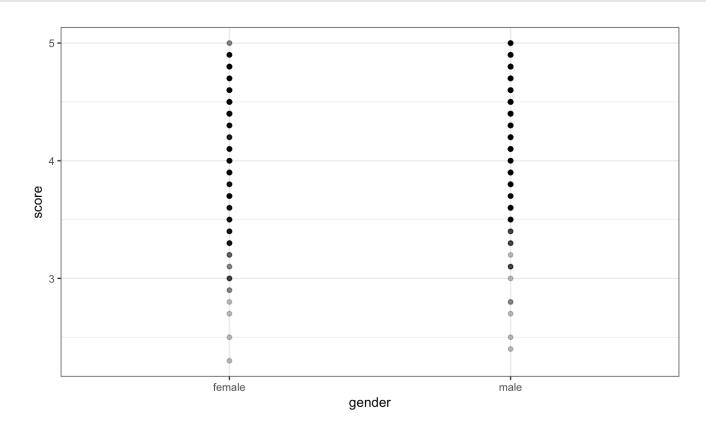




# Regression when the independent variable is a categorical variable

## Relationship between score and gender?

ggplot(evals, aes(x=gender, y=score)) + geom\_point(alpha=0.3) + theme\_bw()



## Regression with gender as the independent variable

```
lm(score ~ gender, data=evals)$coefficients
```

```
## (Intercept) gendermale
## 4.0928205 0.1415078
```

$$\widehat{score} = 4.09 + 0.14 \, gender\_is\_male$$

#### How to interpret the slope:

On average, course evaluation scores for male professors are 0.14 higher than for female professors.

$$\widehat{score} = 4.09 + 0.14 \, gender\_is\_male$$

- · In regression, R encodes categorical independent variables as indicator variables (also called dummy variables).
- R picks a baseline value of the categorical variable. Here the baseline level is female.
- The indicator variable gender\_is\_male is 1 for observations for which gender is male and 0 otherwise.
- · For females,

$$\widehat{score} = 4.09$$

· For males,

$$\widehat{score} = 4.09 + 0.14 = 4.23$$

Could the difference between the mean score for males and females just be due to chance?

The regression model is

$$score = \beta_0 + \beta_1 \ gender\_is\_male + \epsilon$$

where

$$gender\_is\_male = \begin{cases} 1 & \text{if gender is male} \\ 0 & \text{if gender is female} \end{cases}$$

We can answer the question with an hypothesis test with hypotheses

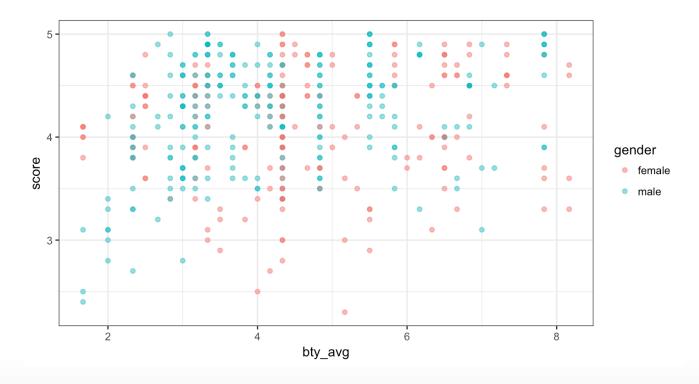
$$H_0: \beta_1 = 0 \text{ versus } H_a: \beta_1 \neq 0$$

```
## Estimate Std. Error t value Pr(>|t|) ## (Intercept) 4.0928205 0.03866539 105.852305 0.0000000000 ## gendermale 0.1415078 0.05882127 2.784422 0.005582967 P Value for text with P_1 = 0
  Strong evidence againet the hull hypothers
so there is evidence of a difference in
Score between male and female professors.
```

Is the regression line the same for two groups?

# Is the relationship between score and bty\_avg the same for male and female professors?

```
ggplot(evals, aes(x=bty_avg, y=score, colour=gender)) +
  geom_point(alpha=0.5) + theme_bw()
```



$$score = \beta_0 + \beta_1 \ gender\_is\_male + \beta_2 \ bty\_avg + \epsilon$$

Model 1 for male professors:

$$score = \beta_0 + \beta_1 + \beta_2 bty\_avg + \epsilon$$

Model 1 for female professors:

$$score = \beta_0 + \beta_2 bty\_avg + \epsilon$$

Same slope different interrept Parallel How would you describe these two lines?

## Fitted parallel lines

```
parallel_lines <- lm(score ~ gender + bty_avg, data=evals)

parallel_lines$coefficients

## (Intercept) gendermale bty_avg
## 3.74733824 0.17238955 0.07415537

Scove = 3.75 + 0.17qwdv-15_male

+ 0.074 bty_avg
```

## Plotting the parallel lines

The augment function (in the library broom) creates a data frame with predicted values (.fitted), residuals, etc. for linear model output.

```
library(broom)
augment(parallel lines)
##
       score gender bty avg
                             .fitted
                                        .se.fit
                                                      .resid
                                                                     hat
                      5.000 4.118115 0.03826883 0.581884899 0.005238155
## 1
         4.7 female
         4.1 female 5.000 4.118115 0.03826383 -0.018115101 0.005238155
## 2
## 3
         3.9 female 5.000 4.118115 0.03826383 -0.218115101 0.005288155
## 4
         4.8 female
                     5.000 4.118115 0.03826383 0.681884899 0.005238155
## 5
         4.6
                      3.000 4.142194 0.038d8791 0.457806096 0.005190100
               male
## 6
                      3.000 4.142194 0.03808791 0.157806096 0.005190100
         4.3
              male
                      3.000 4.142194 0.03808791 -1.342193904 0.005190100
## 7
              male
         2.8
                      3.333 4.166888 0.03551641 -0.066887644 0.004512941
## 8
         4.1
               male
                      3.333 4.166888 0.03551641 -0.766887644 0.004512941
## 9
         3.4
               male
## 10
                      3.167 3.982188 0.04495870 0.517811698 0.007231509
         4.5 female
                      3.167 3.982188 0.04495870 -0.182188302 0.007231509
## 11
         3.8 female
## 12
         4.5 female
                      3.167 3.982188 0.04495870 0.517811698 0.007231509
                      3.167 3.982188 0.04495870 0.617811698 0.007231509
## 13
         4.6 female
                      3.167 3.982188 0.04495870 -0.082188302 0.007231509
## 14
         3.9 female
                                                                                     27/65
                      3.167 3.982188 0.04495870 -0.082188302 0.007231509
## 15
         3.9 female
```

#### Join up the fitted values to plot the parallel lines model

```
ggplot(evals, aes(x=bty avg, y=score, colour=gender)) +
  geom point(alpha=0.5) + theme bw() +
  geom_line(data = augment(parallel_lines), aes(y=.fitted, colour=gender))
                                                              gender
                                                               - female
                                                               -- male
  3
                             bty_avg
```

## Lines for each gender that aren't parallel

Add an independent variable to the model that is the product of gender\_is\_male and bty\_avg. This is called an interaction term.

#### Model 2:

 $score = \beta_0 + \beta_1 \ gender\_is\_male + \beta_2 \ bty\_avg + \beta_3 \ (gender\_is\_male \times bty\_avg) + \epsilon$ 

Model 2 for male professors:

$$score = \beta_0 + \beta_1 + \beta_2 bty\_avg + \beta_3 bty\_avg + \epsilon$$

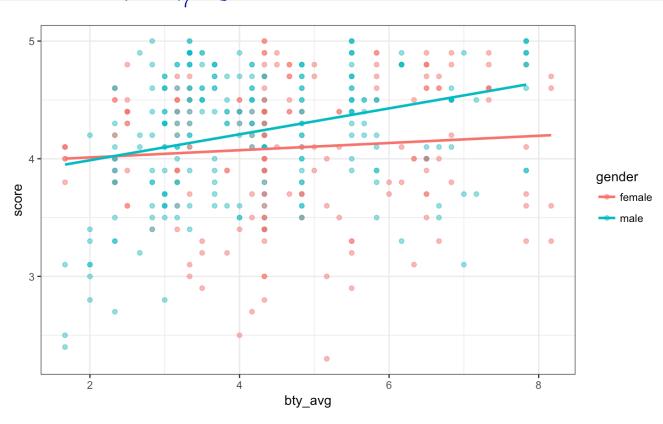
$$score = (\beta_0 + \beta_1) + (\beta_2 + \beta_3) bty\_avg + \epsilon$$

Model 2 for female professors:

$$score = \beta_0 + \beta_2 bty\_avg + \epsilon$$

Both what deflerent and characters interests

## Plot of non-parallel lines



## Fitted lines for male and female professors

Including the term bty avg\*gender on the right-side of the model specification in 1m includes the interaction term plus both of the variables in the model.

summary(lm(score ~ bty avg\*gender, data=evals))\$coefficients ##

3.95005984 0.11799986 33.475124 2.920267e-125 0.03064259 0.02400361 1.276582 2.023952e-01 0.18350903 0.15349459 -1.195541 2.324931e-01 (Intercept)

## gendermale

## bty\_avg:gendermale 0.07961855 0.03246948 2 452105 1.457376e-02

What are the fitted lines for male and for female professors?

## bty avg

score = 3.954 0.03 bty-avg

Score = (3,95-18)+(.03 +0.08)3+y-avg

## Could the difference in the slopes for male and female professors just be due to chance?

Model:

$$score = \beta_0 + \beta_1 \ gender\_is\_male + \beta_2 \ bty\_avg + \beta_3 \ (gender\_is\_male \times bty\_avg) + \epsilon$$

What would be appropriate hypotheses to test?

What do you conclude? Pralue = 0.0146

Some widence against to: \$2 = 0

Conclude that we have some eighered that

the Glope is different for male and female

professors 2/65

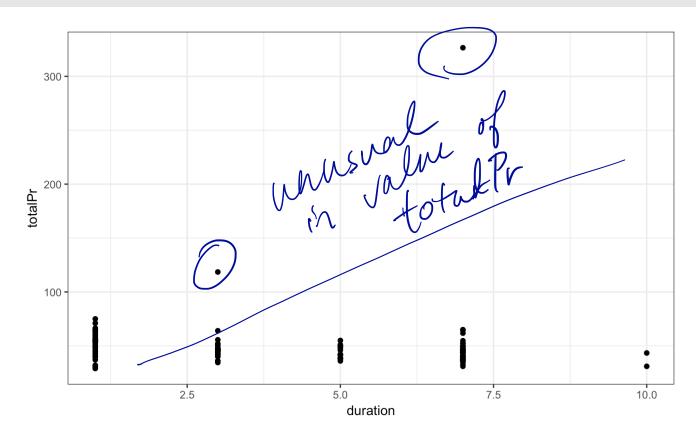
### Example: eBay auctions of *Mario Kart*

- Items can be sold on ebay.com through an auction.
- The person who bids the highest price before the auction ends purchases the item.
- The marioKart dataset in the openintro package includes eBay sales of the game *Mario Kart* for Nintendo Wii in October 2009.
- Do longer auctions (duration, in days) result in higher prices (totalPr)?

## library(openintro) glimpse(marioKart)

```
## Observations: 143
## Variables: 12
## $ ID
                <dbl> 150377422259, 260483376854, 320432342985, 280405224...
## $ duration
                <int> 3, 7, 3, 3, 1, 3, 1, 1, 3, 7, 1, 1, 1, 1, 7, 7, 3, ...
## $ nBids
                <int> 20, 13, 16, 18, 20, 19, 13, 15, 29, 8, 15, 15, 13, ...
## $ cond
                <fctr> new, used, new, new, new, new, used, new, used, us...
                <dbl> 0.99, 0.99, 0.99, 0.99, 0.01, 0.99, 0.01, 1.00, 0.9...
## $ startPr
## $ shipPr
                <dbl> 4.00, 3.99, 3.50, 0.00, 0.00, 4.00, 0.00, 2.99, 4.0...
## $ totalPr
                <dbl> 51.55, 37.04, 45.50, 44.00, 71.00, 45.00, 37.02, 53...
## $ shipSp
                <fctr> standard, firstClass, firstClass, standard, media,...
## $ sellerRate <int> 1580, 365, 998, 7, 820, 270144, 7284, 4858, 27, 201...
## $ stockPhoto <fctr> yes, yes, no, yes, yes, yes, yes, yes, yes, yes, no, ye...
## $ wheels
                <int> 1, 1, 1, 1, 2, 0, 0, 2, 1, 1, 2, 2, 2, 2, 1, 0, 1, ...
## $ title
                <fctr> ~~ Wii MARIO KART & amp; WHEEL ~ NINTENDO Wii ~ BRA...
```

#### ggplot(marioKart, aes(x=duration, y=totalPr)) + geom\_point() + theme\_bw()

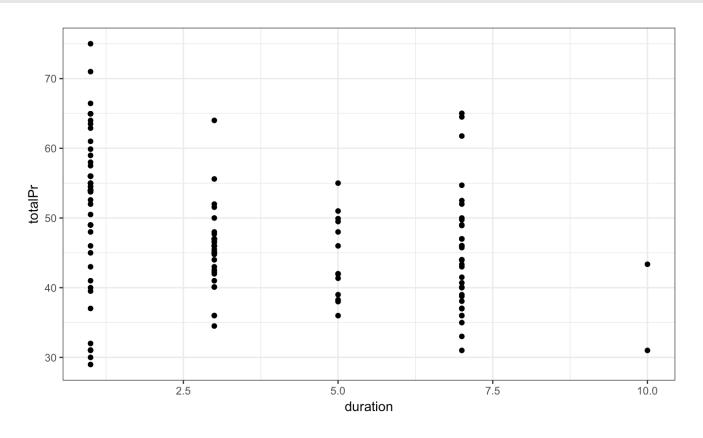


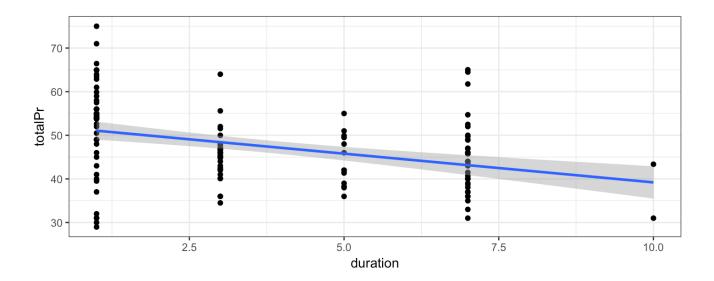
# What should we do with the two outlying values of totalPr?

- Remove outliers only if there is a good reason.
- In these two auctions, and only these two auctions, the game was sold with other items.

```
# create a data set without the outliers
marioKart2 <- marioKart %>% filter(totalPr < 100)</pre>
```

#### ggplot(marioKart2, aes(x=duration, y=totalPr)) + geom\_point() + theme\_bw()





There appears to be a negative relationship between totalPr and duration. That is, the longer an item is on auction, the lower the price.

Does this make sense?

The Would think that longer durattern by higher frices

Maybe there actually isn't a relationship.

We can investigate if the data are consistent with a slope of 0.

```
summary(lm(totalPr ~ duration, data=marioKart2))$coefficients
```

```
## Estimate Std. Error t value Pr(>|t|)
## (Intercept) 52.373584 1.2607560 41.541411 3.010309e-80
## duration -1.317156 0.2769021 -4.756756 4.866701e-06
```

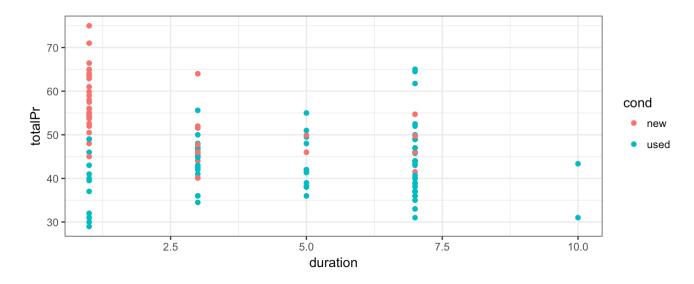
We have strong evidence that the slope is not 0.

P-value = 0.0000049

There must be something else affecting the relationship ...

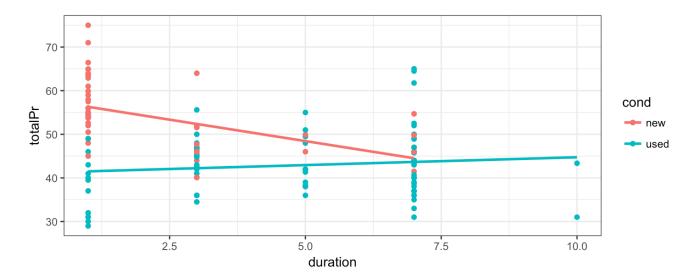
Consider the role of cond. cond is a categorical variable for the game's condition, either new or used.

```
ggplot(marioKart2, aes(x=duration, y=totalPr, color=cond)) +
  geom_point() + theme_bw()
```



New games, which are more desirable, were mostly sold in one-day auctions.

```
ggplot(marioKart2, aes(x=duration, y=totalPr, color=cond)) +
  geom_point() + geom_smooth(method="lm", fill=NA) + theme_bw()
```



- Considering cond changes the nature of the relationship between totalPr and duration.
- This is an example of **Simpson's Paradox** in which the nature of a relationship that we see in all observations changes when we look at sub-groups.

### The fitted lines

summary(lm(totalPr ~ duration\*cond, data=marioKart2))\$coefficients

```
##
                      Estimate Std. Error t value
                                                       Pr(>|t|)
## (Intercept)
                     58.268226 1.3664729 42.641332 5.832075e-81
## duration
                     -1.965595 0.4487799 -4.379865 2.341705e-05
## condused
                    -17.121924 2.1782581 -7.860374 1.013608e-12
## duration:condused 2.324563 0.5483731 4.239016 4.101561e-05
```

For rew games, totally = 58.27 - 1.97 durattra For wed Junes

For Wed Junes

(58.27-17.12)

Lotally = (58.27-1.97) duration

4 (2.32-1.97) duration An example of a variable affecting a relationship between two variables in a non-regression setting:

Data in two-way tables

## A Classic Example: Treatment for kidney stones

Source of data: British Medical Journal (Clinical Research Edition) March 29, 1986

- Observations are patients being treated for kidney stones.
- treatment is one of 2 treatments (A or B)
- · outcome is success or failure of the treatment

Which treatment would you choose?

The table below shows counts of patients being treated for kidney stones.

Which treatment would you choose?

		Treatment A	Treatment B	TOTAL
wy	Success	273	289	562
usfl	Failure	77	61	138
	TOTAL	350	350	700

look at percentages

What would make it easier to decide which treatment is better?

Proportion of observations in each cell in the table:

		Treatment A	Treatment B	TOTAL		
	Success	0.39	0.41	0.80		
	Failure	0.11	0.09	0.20		
_	TOTAL	0.50	0.50	1.00		

John Intern

Proportion of observations in each row and column:

#### Column Percentages

	Treatment A	Treatment B
Success	0.78	0.83
Failure	0.22	0.17

#### **Row Percentages**

	Treatment A	Treatment B
Success	0.49	0.51
Failure	0.56	0.44

proportion of successes in this column (trt A)

#### Proportion of successes in each column:

```
kidney_stones %>%
    count(treatment, outcome) %>%
    group_by(treatment) %>%
    mutate(perc_success = n / sum(n)) %>%
    filter(outcome=="success")

## # A tibble: 2 x 4
## # Groups: treatment [2]
## treatment outcome n perc_success
```

<dbl>

0.7800000

0.8257143

Which treatment would you choose?

<chr> <chr> <int>

A success 273

289

##

## 1

## 2 B success

B Chigher

Successes ... 78%

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## Some vocabulary

*Recall:* The distribution of a variable is the pattern of values in the data for that variable, showing the frequency or relative frequency (proportions) of the occurrence of the values relative to each other.

We can also look at the **joint distribution** of two variables. If both variables are categorical, we can see their joint distribution in a **contingency table** showing the counts of observations in each way the data can be cross-classifed.

$\overline{}$		n	+0	
U	u	Ш	ts	

	Treatment A	Treatment B	TOTAL
Succes	s 273	289	562
Failure	77	61	138
TOTAL	350	350	700

Proportions in the joint distributions:

First table on slide 46

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A marginal distribution is the distribution of only one of the variables in a contingency table.

#### Counts:

	Treatment A	Treatment B	TOTAL
Success	273	289	562
Failure	77	61	138
TOTAL	350	350	700

#### Proportions:

	Treatment A	Treatment B	TOTAL	) distribution	
Success	0.39	0.41	0.80	) distribution	of outcome
Failure	0.11	0.09	0.20		\
TOTAL	0.50	0.50	1.00		
	Marc	shal di	strbut	atment	

A conditional distribution is the distribution of a variable within a fixed value of a second variable.

Column Percentages

Row	Pe	rce	nta	ges
-----	----	-----	-----	-----

	Treatment A	Treatment B
Success	0.78	0.83
Failure	0.22	0.17

	Treatment A	Treatment B
Success	0.49	0.51
Failure	0.56	0.44

What percentage of successes were Treatment A? The Success

Condition on Success

Condition on Success

What percentage of Treatment A surgeries resulted in a success?

condition on treatment 13 A

## Some notation:

Not responsible

 $P(E_1)$  is the probability of an event  $E_1$ 

 $P(E_1 | E_2)$  is the probability of  $E_1$  given that event  $E_2$  has occurred. It is a conditional probability.

#### Example:

- What is the probability it will rain tomorrow?
- What is the probability it will rain tomorrow given that it is raining today?

	Treatment A	Treatment B	TOTAL
Success	0.39	0.41	0.80
Failure	0.11	0.09	0.20
TOTAL	0.50	0.50	1.00

Not responsible

#### **Column Percentages**

Row	Percentages

	Treatment A	Treatment B
Success	0.78	0.83
Failure	0.22	0.17

	Treatment A	Treatment B
Success	0.49	0.51
Failure	0.56	0.44

From the tables, we estimate:

$$P(\text{success}) = 0.80$$

$$P(\text{success} \mid \text{treatment A}) = 0.78$$

$$P(\text{success} \mid \text{treatment B}) = 0.83$$

Does there appear to be a relationship between success and treatment? *Yes! Success is more likely with treatment B.* 

That is, the conditional distribution of one variable is the same for all values of the other variable.

It appears that success and treatment are not independent.

#### Some additional information

- · A is an invasive open surgery treatment
- · B is a new less invasive treatment
- · Doctors get to choose the treatment, depending on the patient
- · What might influence how a doctor chooses a treatment for their patient?

#### Kidney stones come in various sizes

## 3 small A success 81 0.9310345 ## 4 small B success 234 0.8666667

Column percentages:

All Stones

A		В	
Success	0.78		0.83
Failure	0.22		0.17

Which treatment is better?

**Small Stones** 

A	В
0.93	0.87
0.07	0.13

**Large Stones** 

Α	В
0.73	0.69
0.27	0.31

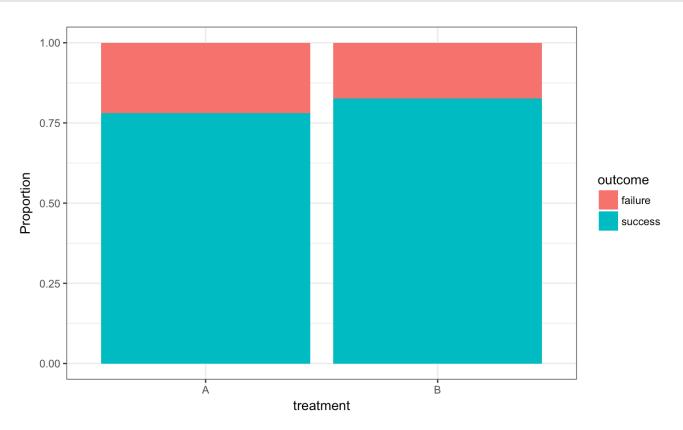
treatment A 15 better (myher success vota) for both small and (any stones This example is another case of **Simpson's paradox**.

#### Moral of the story:

Be careful drawing conclusions from data! It's important to understand how the data were collected and what other factors might have an affect.

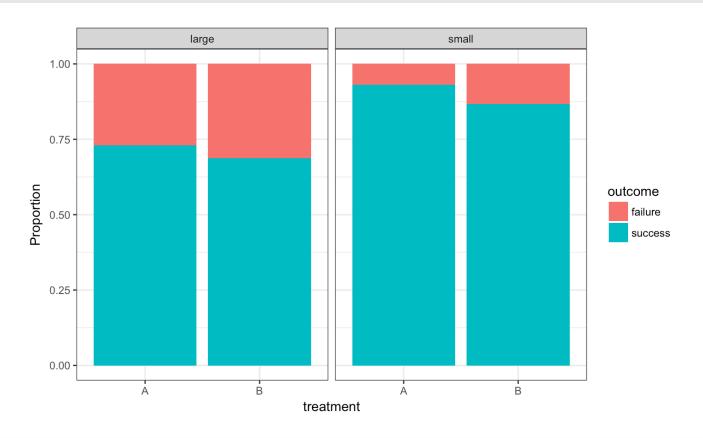
#### Visualizing the kidney stone data: treatment and outcome

```
ggplot(kidney_stones, aes(x=treatment, fill=outcome)) +
  geom_bar(position = "fill") + labs(y="Proportion") + theme_bw()
```



#### Visualizing the kidney stone data: treatment and outcome by size

```
ggplot(kidney_stones, aes(x=treatment, fill=outcome)) + geom_bar(position = "fill") +
    labs(y="Proportion") + facet_grid(. ~ size) + theme_bw()
```



## Confounding

## What is a confounding variable?

- · When examining the relationship between two variables in observational studies, it is important to consider the possible effects of other variables.
- A third variable is a confounding variable if it affects the nature of the relationship between two other variables, so that it is impossible to know if one variable causes another, or if the observed relationship is due to the third variable.
- The possible presence of confounding variables means we must be cautious when interpreting relationships.

#### Examples of situations that may have confounding variables:

- A 2012 <u>study</u> showed that heavy use of marijuana in adolescence can negatively affect IQ.
   Is it possible that there are other variables, such as socioeconomic status, that is associated with both marijuana use and IQ?
- Another 2012 <u>study</u> showed that coffee drinking was inversely related to mortality.
   Should we all drink more coffee so we will live longer? Or is it possible that healthy people, who will live longer because they are healthy, are also more likely to drink coffee than unhealthy people?
- Many nutrition studies.
   Are people who are likely to stick to a diet different than those who won't in important ways?

### How can confounding be avoided?

- Data can be collected through experiments or observational studies.
- · In **observational studies**, data are collected without intervention. The data are measurements of existing characteristics of the individuals being measured.
- In experiments, an investigator imposes an intervention on the individuals being studied, randomly assigning some individuals to one treatment and randomly assigning other individuals to another treatment (sometimes this other treatment is a control).
  - Randomized experiments are often used when we want to be able to say a treatment **causes** a change in a measurement.
  - Other than the difference in treatment received, any differences between the individuals in the treatment and control groups are just due to random chance in their group assignment.

- In a randomized experiment, if there is a difference in our measurement of interest, we can conclude it was caused by the treatment, and not due to some other systematic difference that can confound our interpretation of the effect of the treatment.
- Example experiment from Week 5 lecture:
   Students were randomly assigned to be sleep-deprived or to have unrestricted sleep and how they learned a visual discrimination task was compared between these two groups.
- It's not always practical or ethical to carry out an experiment. For example, you can't randomly assign people to smoke marijuana.

Great care must be taken to deal with potential confounders in observational studies.